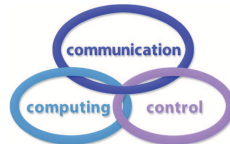


# Parameter Estimation for PMSM based on a Back Propagation Neural Network Optimized by Chaotic Artificial Fish Swarm Algorithm

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**Abstract:** Permanent Magnet Synchronous Motor(PMSM) control system with strong nonlinearity makes it difficult to accurately identify motor parameters such as stator winding,  $dq$  axis inductance, and rotor flux linkage. Aiming at the premature convergence of traditional Back Propagation Neural Network(BPNN) in PMSM motor parameter identification, a new method of PMSM motor parameter identification is proposed. It uses Chaotic Artificial Fish Swarm Algorithm(CAFSA) to optimize the initial weights and thresholds of BPNN, and then strengthens training by BPNN algorithm. Thus, the global optimal network parameters are obtained by using the global optimization of CAFSA and the local search ability of BPNN. The simulation results and experimental data show that the initial value sensitivity of the network model optimized by CAFS-BPNN Algorithm is weak, the parameter setting is robust, and the system stability is good under complex conditions. Compared with other intelligent algorithms, such as RSL and PSO, CAFS-BPNN has high identification accuracy and fast convergence speed for PMSM motor parameters.

**Keywords:** Permanent Magnet Synchronous Motor(PMSM), Back Propagation Neural Network(BPNN), Chaotic Artificial Fish Swarm Algorithm(CAFSA), parameter estimation, identification accuracy, convergence speed.

## 1 Introduction

Permanent magnet synchronous motor (PMSM) is widely used in industrial robots, servo drive control, electric vehicle speed regulation and other high-precision control fields due to its outstanding advantages in power and torque density, speed control performance and system robustness [10].

PMSM motor parameters include stator windings, dq axis inductance, rotor flux, etc. They can be used to reflect the performance of the motor system during operation, and can assist to complete motor condition monitoring [5] and fault diagnosis [12]. Therefore, accurate parameter identification ability is very important for motor control system.

However, motor parameters are very vulnerable to external factors such as temperature, flux saturation and skin effect [3], such as temperature change will affect the stator winding, permanent magnet demagnetization directly affects the dq axis inductance [22]. With the change of working condition and surrounding environment, there is a certain difference between actual parameters and nominal parameters [17].

Therefore, as a motor controller, it must have the function of self-tuning and identification of motor parameters. Considering the technical difficulty and cost, it is difficult to directly measure motor parameters through auxiliary sensors such as temperature and magnetism [5, 15].

PMSM control system has very strong non-linear and time-varying characteristics. It is very difficult to accurately identify the parameters of PMSM. The identification algorithm needs to comprehensively weigh the factors of complexity, convergence and computing time.

## 2 Related works

In traditional control theory, parameter identification methods of PMSM include least square method (RLS) [18, 23], extended Kalman filter identification (EKF) [1, 6, 20], model reference adaptive (MRAS) [2, 26] etc.

Because of the linear parameterization of RLS algorithm, RLS estimators are usually noise sensitive, which may lead to lower identification accuracy. When estimating the winding resistance and rotor flux by EKF, the estimator is noisy and unstable, so it can not accurately estimate the actual parameters.

MRAS estimator can not accurately estimate winding resistance, inductance and rotor flux simultaneously. It is often impossible to find the optimal solution of the estimated parameters accurately by using the above methods. With the development of swarm intelligence theory, many scholars have applied this kind of optimization algorithm to motor parameter identification, including ant colony algorithm [4], genetic algorithm [21], particle swarm optimization algorithm [14]. Ant colony algorithm and particle swarm optimization algorithm are easy to fall into local optimization convergence, and the optimization error is relatively large. Literature [11] uses genetic algorithm to identify  $dq$  axis inductance and rotor flux, because of the large space-time complexity, the convergence speed is slow. Literature [14] uses dynamic particle swarm optimization (DPSO-LS) algorithm and dynamic anti-learning strategy of Gauss distribution to enhance the global search ability, but the computational complexity becomes larger.

With the development of artificial intelligence technology, the artificial neural network is widely used in parameter identification of PMSM motor, and BPNN is the most widely used [21, 25].

BPNN is a multi-layer feedforward neural network trained by error back propagation algorithm. It has the advantages of clear model structure and simple calculation. It has been proved theoretically that its three-layer model can map any complex non-linear relationship model [16]. It is widely used in non-linear curve fitting in various signal processing and automatic control.

BPNN has excellent local optimization ability and can converge quickly and accurately in local areas. However, this advantage has also results in poor global search performance, local prematurity, poor global convergence, long iteration period and other problems, and its algorithm optimization is difficult to achieve the desired convergence accuracy and convergence speed. Therefore, it is necessary to combine the BPNN algorithm with the other intelligent algorithm with stronger global optimization ability. In the early stage of training, the cooperative algorithm is used to converge the network to the global extremum quickly, and then the local optimization characteristic of BPNN is used to converge quickly.

CAFSA is a swarm intelligence algorithm with excellent global searching ability. It simulates the behavior of fish swarm such as preying, swarming, following and moving to optimize the system. It has the characteristics of weak sensitivity to initial values, strong robustness to parameter setting, good global searching performance and fast convergence speed [19, 23].

CAFSA algorithm has large randomness and poor convergence in the later search period. It needs to improve the optimization performance by improving system step size, the field of view, adding congestion factor [8]. The combination of CAFSA and BPNN will make up for their respective optimization shortcomings, and improve the overall optimization performance in terms of convergence speed and accuracy.

This paper presents a PMSM motor parameter identification algorithm based on CAFS-BPNN, which combines BPNN with AFSA effectively. By injecting impulse current into the d-axis of PMSM motor control system, the sampling process data, including d-axis voltage, q-axis voltage, d-axis current, q-axis current and motor speed, are used as data sets for network training and testing. The parameters set  $\{R_s, L_d, L_q, \psi_f\}$  to be identified are taken as network output. Combining the global search ability of CAFSA and the local fast convergence property of BPNN, the convergence accuracy and speed of PMSM motor parameter identification are effectively improved.

The outstanding contributions of this paper include:

(1) Using the forward propagation topology of BPNN, a nonlinear mapping identification model from sampled parameter set  $\{u_d, u_q, i_d, i_q, \omega\}$  to identified parameter set  $\{R_s, L_d, L_q, \psi_f\}$  of permanent magnet synchronous motor (PMSM) is constructed. The input data set of the mapping model is obtained by d-axis current injection method, and parameters of PMSM motor to be identified are obtained by simple and direct mapping model.

(2) The CAFS-BPNN algorithm of BPNN optimized by CAFSA is introduced into online identification of PMSM motor parameters. The connection weights and thresholds of BPNN network are taken as the optimization objects of CAFSA. The connection weights and thresholds of BPNN are optimized quickly by using CAFSA global search ability in the early stage of training, and then the optimization of BPNN is transferred to the global optimal extremum point in the later stage. By giving full play to their respective optimization characteristics and avoiding their own shortcomings, the convergence accuracy and speed of obtaining network parameters of PMSM motor parameter identification model are effectively improved.

(3) The population aggregation degree is embedded in CAFS-BPNN as the switching condition of the two intelligent algorithms. According to the optimization characteristics of the fish swarm algorithm, the aggregation degree of the population increases in the later stage of optimization. When it reaches the preset threshold, it means that it reaches the late stage of fast convergence optimization algorithm of CAFSA, and can be transferred to BPNN precision optimization algorithm, thus the time of turning into precision optimization algorithm is accelerated.

### 3 Theoretical analysis of group intelligence identification model for PMSM motor parameters

#### 3.1 Mathematical model for PMSM motor identification

PMSM control system is a complex system with strong coupling and time-varying nonlinearity. It can establish mathematical models in static three-phase coordinate system, static  $\alpha\beta$  coordinate system and synchronous rotating  $dq$  coordinate system. The mathematical models in three coordinate systems can be transformed each other. The mathematical model in the  $dq$  coordinate system is the most commonly used mathematical model [11].

Neglecting the magnetic saturation effect of PMSM and the eddy current and hysteresis loss of core are neglected, the voltage equation and flux linkage equation in the  $dq$  coordinate system are expressed as (1) and (2):

$$\begin{cases} u_d = R_s i_d + \frac{d\psi_d}{dt} - \omega \psi_q \\ u_q = R_s i_q + \frac{d\psi_q}{dt} - \omega \psi_d \end{cases} \quad (1)$$

$$\begin{cases} \psi_d = L_d i_d + \psi_f \\ \psi_q = L_q i_q \end{cases} \quad (2)$$

where  $u_d$  and  $u_q$  are the voltage component on the  $dq$  axis,  $i_d$  and  $i_q$  are the current component on the  $dq$  axis,  $R_s$  is the stator resistance,  $\psi_d$  and  $\psi_q$  are the flux linkage on the  $dq$  axis,  $L_d$  and  $L_q$  are the inductance on the  $dq$  axis,  $\psi_f$  is the flux chain generated by the permanent magnet,  $\omega$  is the electrical angular speed.

In the synchronous rotating  $dq$  coordinate system, the mathematical model of PMSM can be expressed as:

$$\begin{cases} \frac{di_d}{dt} = \frac{R_s}{L_d} i_d + \frac{L_q}{L_d} \omega i_d + \frac{u_d}{L_d} \\ \frac{di_q}{dt} = \frac{R_s}{L_q} i_q + \frac{L_d}{L_q} \omega i_d + \frac{u_q}{L_q} - \frac{\psi_f}{L_q} \omega \end{cases} \quad (3)$$

$p = \{R_s, L_d, L_q, \psi_f\}$  is the set of parameters that need to be identified synchronously.

When  $i_d = 0$ , the  $dq$  axis current is decoupled so that the stator current has only the AC component of  $q$  axis. In the steady state, formula (2) is brought into formula (1) and discretized to express as follows:

$$\begin{cases} u_{d0} = -L_q \omega_0 \psi_{q0} \\ u_{q0} = R_s i_{q0} + \psi_{f0} \omega_0 \end{cases} \quad (4)$$

Formula (4) shows that the order of the motor equation is two, but the system needs to identify four parameters:  $\{R_s, L_d, L_q, \psi_f\}$ .

The equation of state is rank-deficit type. By injecting the d-axis current of instantaneous  $i_d \neq 0$  into the steady state, the motor model is expressed as:

$$\begin{cases} u_{d1} = R_s i_{d1} - L_q \omega_1 i_{q1} \\ u_{q1} = R_s i_{q1} + L_d \omega_1 i_{d1} + \psi_f \omega_1 \end{cases} \quad (5)$$

It can be seen from literature [2] that the measurement error of rotor flux linkage  $\psi_{ferror}$  is caused by assuming  $L_d = L_q$  and  $\psi_f = \psi_{f0}$ .

When  $\psi_{ferror}$  is negligible relative to  $\psi_{f0}$ , (12) shows that  $\psi_{fe}$  and  $\psi_{f0}$  are equal, and  $|\psi_{ferror}|$  can be simplified as follows:

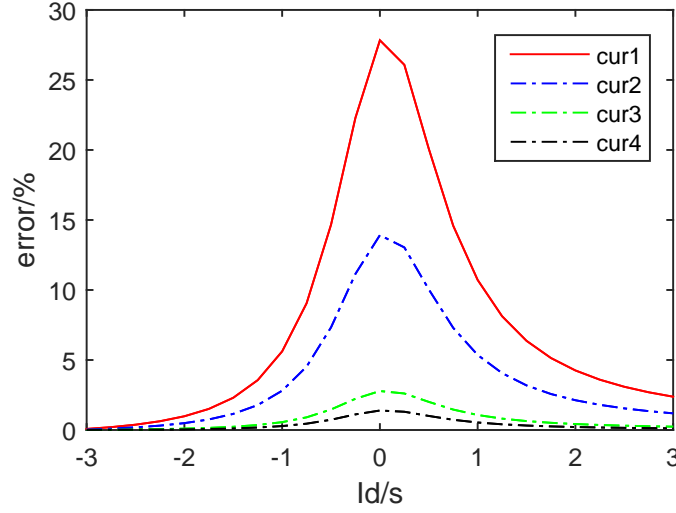


Figure 1: Estimation error of rotor flux relative to d-axis current

$i_q = 3.55A, i_{q0} = 3.35A, \psi_{m0} = 175Wb, L_d = 8.5mH$  Cure1: $\Delta\psi_m = 1\%\Delta\psi_{m0}, \Delta L = 10\%L_d$   
Cure2: $\Delta\psi_m = 0.5\%\Delta\psi_{m0}, \Delta L = 5\%L_d$  Cure3: $\Delta\psi_m = 0.1\%\Delta\psi_{m0}, \Delta L = 1\%L_d$  Cure4: $\Delta\psi_m = 0.05\%\Delta\psi_{m0}, \Delta L = 0.5\%L_d$

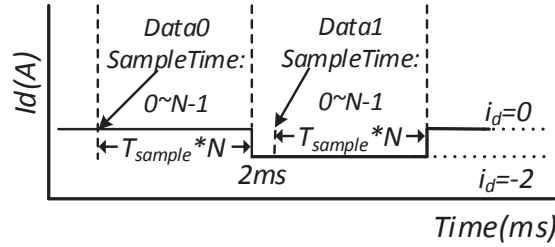


Figure 2: Time series model for data sampling

$$|\psi_{ferror}| \approx \left| \frac{\Delta\psi_f i_{q1}^2 + \Delta L i_{d1} i_{q1}^2}{i_{q1}^2 - i_{d1}^2 - i_{q1}^2} \right| = \left| \frac{\Delta\psi_f i_{q1}^2}{i_{d1}^2} + \frac{\Delta L i_{q1}^2}{i_{d1}} \right| \quad (6)$$

When  $i_{d1}$  is large enough, (13) shows that  $|\psi_{ferror}| \rightarrow 0$  and  $\psi_{fe} \approx \psi_{f0}$ , see Fig. 1.

### 3.2 Data set acquisition method of PMSM motor identification model

Generally, PMSM motors can be controlled by constant torque angle (torque angle is  $90^\circ$ ). Adjusting the  $d$ -axis current ( $i_d = 0$ ) makes the  $q$ -axis get the maximum torque.

In order to obtain the information of motor speed,  $dq$  axis current and voltage needed to be sampled when evaluating motor parameters, Data0 and Data1 were obtained by alternately adjusting ( $i_d = 0$ ) and ( $i_d \neq 0$ ) injecting reverse  $d$  axis current ( $i_d = -2A$ ) during sampling period.

The single sampling time is  $T_{sample} (= 10^{-4}s)$ , and the total sampling time is  $T_{sample} * N$ .

The time series model of data sampling is shown in Fig.2. Data1 data sampling start time is 2ms after current switching, which avoids the interference caused by current switching and ensures the stability of sampling data.

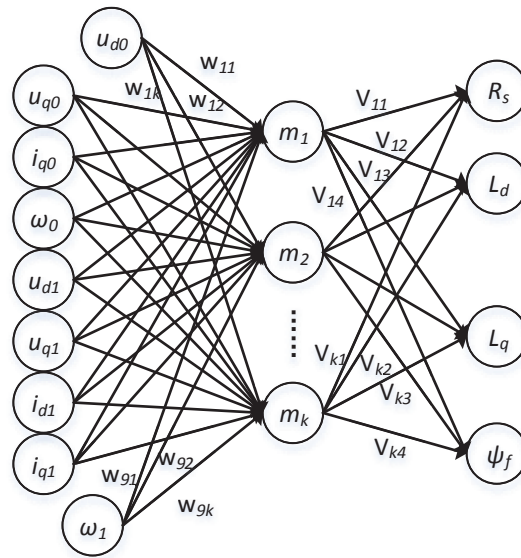


Figure 3: BPNN-PMSM motor parameter identification model

### 3.3 Parameter mapping model of PMSM motor identification based on BPNN

According to the principle of BPNN and the control strategy model of PMSM in Section 3.1, the set  $\{R_s, L_d, L_q, \psi_f\}$  of PMSM parameters to be identified is taken as the output neuron set of BPNN, and the  $data0 = \{u_{d0}, u_{q0}, i_{q0}, \omega_0\}$  ( $i_d = 0$ ) and  $data1 = \{u_{d1}, u_{q1}, i_{d1}, i_{q1}, \omega_1\}$  ( $i_d \neq 0$ ) are used as the input neuron set.

The BPNN parameter identification model of PMSM motor as shown in Fig. 3 is constructed.

The three-layer neural network model consists of nine input neurons and four output neurons. The hidden layer uses Tansig function as the transfer function  $f_1(\cdot)$ , and the output layer uses linear purelin as the transfer function  $f_2(\cdot)$ .

The hidden layer neurons output  $z_h = f_1(\sum_{i=0}^n \omega_{ih} x_i)$  ( $h = 1, 2, \dots, 9$ ) and the output layer neurons output  $y_j = f_2(\sum_{h=0}^m v_{hj} z_h)$  ( $j = 1, 2, 3, 4$ ), thus the BPNN network completes the mapping from the input 9-dimensional space to the output 4-dimensional space.

After determining the input layer, output layer and data set of BPNN network, the key factors affecting the performance of BPNN network include the number of hidden layer layers, the number of hidden layer neurons, initial connection weights and thresholds, learning rate and learning algorithm. Increasing the hidden layer can reduce the network error and improve the accuracy, but the performance will also increase the network complexity and training time, and may appear the tendency of "over-fitting". According to Hornic's theory that three-layer BPNN can fit arbitrary non-linear curve, the identification model in this paper adopts a three-layer network structure with one hidden layer. The number of hidden layer neurons directly determines whether the network will appear "over-fitting" phenomenon, but there is no theory to accurately determine the number of hidden layer neurons in BPNN network. In this paper, empirical formula and experimental verification will be used to determine the optimal number.

The setting of initial connection weights and thresholds will have a great impact on the convergence speed of the model.

In this paper, the artificial fish swarm algorithm with strong initial robustness is introduced into the initial optimization of the model, so as to improve the convergence speed and speed up

the global optimization.

Through the study of BPNN network, the following empirical formulas for calculating hidden layer neuron data are formed:

Gagan pointed out the logarithmic relationship between the hidden layer neurons and the input neurons.

Formula 1:  $m_1 = \log_2 n$  [20]. Kolmogorov's theorem shows that there exists a relationship between recessive neurons and input neurons.

Formula 2:  $m_2 = 2n - 1$ . D. Gao [7] used least square method to simplify the relationship between input and output and hidden layer neurons.

Formula 3:  $m_3 = \sqrt{(0.43nl + 0.12l^2 + 2.54n + 0.77l + 0.35) + 0.51}$  [7]. The number of hidden layer neurons can be calculated by input neurons and output neurons.

Formula 4:  $m_4 = \sqrt{nl}$ . The number of neurons in the hidden layer was obtained by using input neurons and output neurons as well as by adjusting parameters.

Formula 5:  $m_5 = \sqrt{n+l} + \alpha, \alpha = 1, 2, \dots, 10$ . In the above formula, m is the number of neurons in the hidden layer, n is the number of neurons in the input layer, l is the number of neurons in the output layer.

Table 1: The number of neurons in the hidden layer of BPNN

No.	$m_1$	$m_2$	$m_3$	$m_4$	$m_5$	m
$n = 9, l = 4, \alpha = 1, 2, \dots, 10$	4	17	8	6	5-14	4-17

The number of hidden layer neurons  $m = m_1, m_2, m_3, m_4, m_5$  is obtained by combining the above empirical formulas. According to the BPNN-PMSM parameter identification model in Chapter 3.3,  $n = 9, l = 4$  can be obtained. The number of hidden layer neurons m is shown in Tab.1.

Weight Mean Square Error (WMSE) is used to calculate the training errors.

The individual error of sample p can be expressed:

$$E_p = \frac{1}{2} \sum_{j=1}^l (\hat{y}_j^p - y_j^p)^2 w_j, \text{ and global error WMSE can be expressed: } WMSE = \sum_{i=1}^p E_p.$$

In the previous two formulas, l is the number of output nodes, p is the number of training samples,  $\hat{y}_j^p$  is the expected output value of network,  $y_j^p$  is the actual output value of network, and  $w_j$  is the error weight of output nodes.

According to the definition of net input value  $S_j$  of neuron node  $y_j$ , the hidden layer neuron output  $z_h = f_1(S_h)$  and the output layer neuron output  $y_j = f_2(S_j)$  described in chapter 3.3.

$v_{hj}$  is the weights of output layer connection and  $w_{ih}$  is hidden layer connection. They can be adjusted by cumulative error algorithm.

The increments of connection weight  $\Delta v_{hj}$  and  $\Delta w_{ih}$  can be generated after each iteration.

They are expressed as follows:

$$\Delta v_{hj} = \sum_{i=1}^p \sum_{j=1}^l \eta (\hat{y}_j^p - y_j^p)^2 f_2'(S_j) z_j, \Delta w_{ih} = \sum_{i=1}^p \sum_{j=1}^l (\eta (\hat{y}_j^p - y_j^p)^2 f_2'(S_j) v_{hj} f_1'(S_h) x_i,$$

where  $\eta$  is learning rate and  $\eta \in (0.01, 10)$ .

In the process of learning, the weighted inertial momentum is used to reduce the learning oscillation and accelerate the convergence of the system.

The adjusted formula for calculating the actual weights can be expressed:

$$\Delta w(n) = -\eta_1 \Delta WMSE(n) + \alpha w(n-1), \text{ where } \eta_1 \text{ is learning rate and } \alpha \text{ is the inertial momentum.}$$

In order to adapt the BPNN network to the convergence speed in different periods, the system learning rate parameter  $\eta_1$  is adjusted dynamically and adaptively.

The error ratio can be expressed:

$$\varphi = WMSE(n) / WMSE(n-1).$$

When  $\varphi$  is larger than the threshold value  $\varphi_{th}$ , the learning rate is increased, and vice versa, which ensures that the learning rate is earlier and faster in the early learning stage.

In the later stage of learning, the learning rate decreases, the vibration decreases and tends to be optimal.

Table 2: Relationships between hidden layer neurons and errors

Hidden layer neuron	Training error (%)	Testing error (%)	Hidden layer neuron	Training error (%)	Testing error (%)
4	12.6334	12.0542	11	8.2683	7.0547
5	10.4325	10.1453	12	7.5876	6.2482
6	10.0836	9.2695	13	7.0218	5.0624
7	9.5836	9.0521	14	6.6482	6.1486
8	9.0452	8.8485	15	5.8473	5.1862
9	8.6142	8.5858	16	5.8593	5.8864
10	8.056	8.1524	17	5.7324	5.3485

The data set is acquired by sampling model in section 3.2. The sampling times is 500. 400 sets of data are used as training set and the others are used as test set. The data of hidden layer neurons are set to 4-17. Because the parameters of four output neurons involved in this paper are equally important in motor performance evaluation, the training and testing results are shown in Tab.2 according to the average weight. The error data show that with the increase of the number of hidden layer neurons, the training error and test error decrease gradually, but the test error fluctuates when the number of hidden layer neurons exceeds 11. The number of hidden layer neurons can be set at 13-15 in the comprehensive comparison error data, which is selected as 15 in this paper.

### 3.4 Chaos artificial fish swarm algorithm

In this paper, the Chaos Artificial Fish Swarm Algorithms (CAFSA) algorithm is used to optimize BPNN, and a PMSM motor parameter identification model based on CAFSBPNN algorithm is proposed.

#### Relevant definitions of CAFSBPNN algorithms

The state of individual AF fish in artificial fish swarm at time  $t$  is defined as:  $X_S(t) = (x_1^S(t), x_2^S(t), \dots, x_D^S(t))$ , ( $S = 1, 2, \dots, AF\_Num$ ).

where  $AF\_Num$  is the size of artificial fish,  $D$  is the state dimension of  $X_S(t)$  (the sum of connection weights and thresholds of BPNN),  $x_i^S(t)$  ( $i = 1, 2, \dots, D$ ) are variables waiting for optimization.  $E_S(t) = \frac{1}{e_S(t)}$  is the current food concentration of  $S$ th artificial fish.

$Visual$  is the visual range of artificial fish (perceived distance),  $Step$  is moving step of artificial fish,  $\Delta$  is crowding factor.

CAFSBPNN is a three-layer BPNN network with one hidden layer, in which the number of neurons in the input layer ( $L_{in}$ ) is  $n = 9$ , the number of neurons in the hidden layer ( $L_h$ ) is  $m = 15$ , and the number of neurons in the output layer ( $L_o$ ) is  $l = 4$ .

The dimension  $D$  of  $X_S(t)$  of artificial fish can be calculated as:  $D = m(n + 1) + l(m + 1) = 15 * 10 + 4 * 16 = 216$ .

The connection weights of  $L_{in} \rightarrow L_h$  and  $L_h \rightarrow L_o$  in BPNN are assigned to the front part of  $X_S(t)$ , and the thresholds of neurons in  $L_h$  and  $L_o$  are stored in the back part of  $X_S(t)$ .



Individual fish  $X_S(t)$  contains the connection weights and thresholds needed to construct BPNN network, which can represent a BPNN.

When AF is initialized,  $AF\_Num$  of the artificial fish are put in the range of [-1,1] by chaotic random mode.

Initial fish food concentration  $E_S(t) = \frac{1}{e_S(t)}$ , where  $e_S(t) = \frac{WMSE}{N}$ ,  $WMSE$  is the global weighted mean square error, and  $N$  is the dimension of training sample set.

The smaller the error  $e_S(t)$  between the expected output value and the actual output value of the network, the higher the food concentration  $E_S(t)$  of the artificial fish, and the better the performance of the neural network constructed by the artificial fish.

The distance  $d_{PQ}$  between any two artificial fish  $X_P(t)$  and  $X_Q(t)$  in AF is calculated as follows:

$$d_{PQ} = \frac{\sum_{i=1}^D |X_i^P(t) - X_i^Q(t)|}{D}, \quad X_i^P(t), X_i^Q(t) \text{ is the corresponding state value of two artificial fish.}$$

When  $d_{PQ} < Visual$ ,  $X_P(t)$  and  $X_Q(t)$  are the corresponding state values of two artificial fish.

### Behavior description of artificial fish swarm algorithms

(a) *Prey behavior*: Fish tend to move towards high food concentration in water through their sensory organs.

Artificial fish  $X_i(t)$  traverses all the partner fish in the search field, and the number of partners  $Frd\_Num$  was calculated.

At first, the target fish  $X_{target}(t)$  is assigned  $X_i(t)$ , and the food concentration is compared with that of partner fish  $X_j(t)$  in each traverse. If  $E_{target}(t) < E_j(t)$ , the target fish to be searched is recorded as partner fish  $X_j(t)$ .

After searching all the partner fish, if the target fish  $X_{target}(t)$  is found, then the artificial fish  $X_i(t)$  moves one step to the  $X_{target}(t)$  according to:  $X_i(t+1) = X_i(t) + rounds() \cdot step \cdot \frac{X_{target}(t) - X_i(t)}{d_{targeti}}$ ; otherwise, the artificial fish  $X_i(t)$  moves one step to the cluster center.

(b) *Swarm behavior*: Fish like to gather, forage collectively and avoid risks. Assuming that the current state of artificial fish is artificial fish  $X_i(t)$ , the number of companion fish  $Frd\_Num$  and the central position  $X_c(t)$  are obtained by traversing the search field.

If  $\frac{E_c(t)}{Frd\_Num} > \Delta E_i(t)$ , it means that the food concentration in the partner center is high but not too crowded.

It can move forward to the center according to:  $X_i(t+1) = X_i(t) + rounds() \cdot step \cdot \frac{X_c(t) - X_i(t)}{d_{ci}}$ , otherwise preying behavior will be carried out.

(c) *Fellow behavior*: Some individuals in the fish swarm find the food and share the location, and others follow and arrive at the food point to eat together.

Assuming that the current state of artificial fish is  $X_b(t)$ , the number of partners in the field of vision is  $Frd\_Num$  and the highest concentration of food is  $X_b(t)$ .

If  $\frac{E_b(t)}{Frd\_Num} > \Delta E_i(t)$ , it shows that the partner with the highest food concentration is not too crowded at  $X_b(t)$ .

At this time,  $X_i(t)$  can move towards partner  $X_b(t)$  according to:  $X_i(t+1) = X_i(t) + rounds() \cdot step \cdot \frac{X_b(t) - X_i(t)}{d_{bi}}$ ; otherwise, preying behavior will be carried out.

(d) *Moving behavior*: When the individual fish  $X_i(t)$  in the fish swarm finds that there is no other partner around them, it can move randomly to the next position within its field of vision according to:

$X_i(t+1) = X_i(t) + \text{rounds}() \cdot \text{step}$ , thus widening the range of swarming, and further exploring for obtaining global optimum.

(e) *Bulletin board*: Update and preserve the highest food concentration and the corresponding individual fish status. In the iteration traversal process, when the individual fish food concentration is higher than the bulletin board record, the bulletin board is updated.

### Chaotic search

Chaotic phenomena refer to irregular and unpredictable behaviors in non-linear systems, which are ergodic and random. When chaotic search is introduced into AFSA algorithm, its ergodicity can make the fish swarm search range include the whole target area, and its randomness is conducive to the search process breaking away from local extremum and tending to global optimum, which improves the search efficiency of AFSA algorithm and shortens the convergence time of global optimization.

Typical chaotic systems include Logistic mapping, Lorenz system and Henon map. In this paper, one-dimensional logistic chaotic system is used as the random motion behavior required in the search process of AFSA.

Definitions are as follows:  $y_{k+1} = f(\mu, y_k) = \mu y_k(1 - y_k)$ , where,  $y_k \in (0, 1)$  and it is the value of  $y$  after  $k$ th iterations, and  $\mu$  is the control parameter of the system.

When  $\mu = 4$ , the system is in a completely chaotic state, at which time  $y_k$  can not repeat all the values between  $(0, 1)$ .

Logistic chaotic system optimizes the activities of artificial fish swarm.

It means that the generation of all random numbers includes the initialization of artificial fish and the activities of fish swarm. Therefore, the following provisions are made for artificial fish swarm:

(a) The chaotic system generates the initial artificial fish. There are 216 initial connection weights and thresholds to be optimized in the parameter identification model of permanent magnet synchronous motor based on CAFSNNA.

For the  $i$ -th Artificial Fish  $X_i(t)$ , the chaotic variable  $y_{ik}(k = 1, 2, \dots, 216)$  is generated by using the logistic system, and the initial value  $X_i(0)$  is set accordingly.

If the range of parameters to be identified is  $(a, b)$ , the initial state of artificial fish  $X_i(0)$  is:  $X_i(0) = (x_1^i(0), x_2^i(0), \dots, x_{216}^i(0))$ , where  $x_k^i(0) = a_i + (b_i + a_i)y_{ik}$ .

Similarly,  $AF\_Num$  artificial fish can be produced.

(b) The random number function  $\text{rounds}()$  used in formula (14-17) is generated by logistic chaotic system when calculating the preying, swarming, following and moving behavior of artificial fish swarm.

## 4 Process analysis of PMSM motor parameter identification network algorithm based on CAFSPNNA

### 4.1 Network optimization algorithm for PMSM motor parameter identification based on CAFSBPNN

CAFSPNN includes two parts for PMSM motor parameter identification. In the early stage, the superior global optimization ability of chaotic artificial fish swarm is used to quickly approach the global optimal point. In the later stage, the fast local convergence of BPNN neural

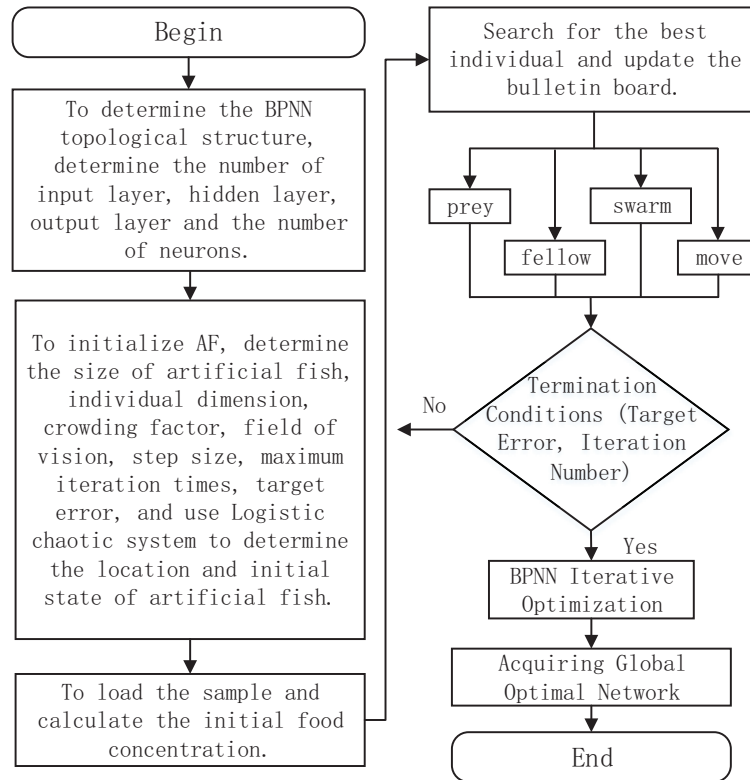


Figure 4: Procedure of PMSM motor parameter identification based on CAFSBPNN

network is used to complete the final global optimal point. The specific steps are as follows (see Fig. 4).

(1) Initialize BPNN: According to the PMSM motor parameter evaluation model, the BPNN network topology structure is determined: the number of input layer, hidden layer, output layer and the number of their respective neurons.

(2) Initialize CAFS: According to the topological structure of BPNN network, the connection weights and thresholds are determined. Set the initial state value of artificial fish: fish size( $AF\_Num$ ), individual fish state dimension( $D$ ), visual range( $Visual$ ), moving step( $step$ ), crowding factor( $\Delta$ ), maximum iteration number( $i_{max}$ ), target error( $WMSE_{max}$ ).

Logistic chaotic system is used to determine the position and initial state of artificial fish. The initial position of individual fish  $X_i(0)$  and corresponding food concentration  $E_i(0)$  were calculated by loading samples data.

(3) Update bulletin board: The highest food concentration of individual fish was selected by traversing comparison, and the Bulletin Board was judged and updated.

(4) Behavior selection of AF: Fish swarm chooses and executes four kinds of activities: preying, following, swarming and moving. Logistic chaotic system is used to enter the next optimal position.

(5) CAFS termination condition judgment: According to the Bulletin Board, the optimal food concentration and the number of iterations, it is judged whether the CAFS termination condition of CAFSNNA optimization is satisfied, and then it is transferred to the later BPNN optimization, otherwise the next step (3) is to continue the fish optimization.

(6) BPNN optimization: Transfer to the BPNN iterative optimization process, using the aforementioned BPNN back propagation iteration weight updating method until the final opti-

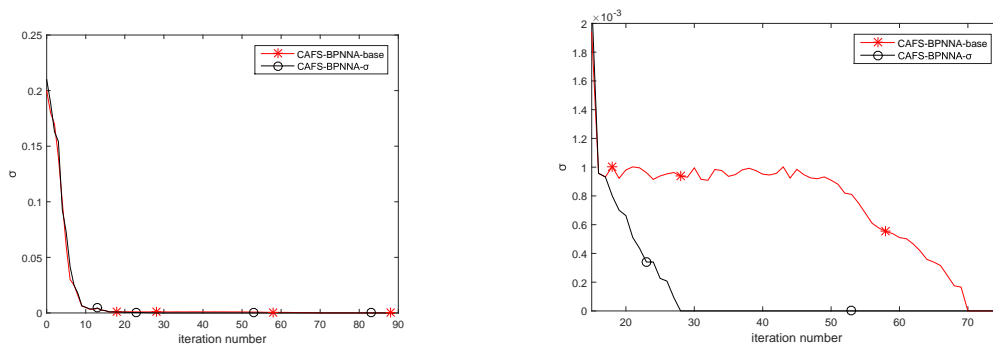


Figure 5: Aggregation degree  $\sigma$  of optimized iterative population based on CAFSBPNNa

mization conditions are satisfied to obtain the global optimal network.

#### 4.2 Selection of switching opportunity for two swarm intelligence algorithms in CAFSBPNNa network optimization

In the identification model, the optimization process of BPNN network parameters is completed by CAFS and BPNN algorithms in two stages. If the switching point is too late, the CAFS algorithm will produce blind search when it approaches the global extremum point in the later stage, which will affect the convergence speed. On the contrary, if the switching point is too early and enters the BPNN search process too early, it will lead to premature convergence to the local extremum point, which will affect the convergence accuracy.

Therefore, accurately grasping the switching time of the two algorithms is very important for the whole optimization. In the traditional CAFS algorithm, the termination conditions are mainly determined by the number of iterations and the target error, but in the optimization process of CAFSNNA fusion algorithm, it is difficult to accurately judge whether it has entered the optimal terminal of CAFS fast convergence by only a single system target error.

In the later stage of CAFS algorithm, the individual fish in the population are clustered near the global extremum because of their preferential characteristics, so the individual aggregation degree of the population is obviously increased, and the individual fitness value of each individual fish will also approach the average fitness value of the system.

For this reason, the aggregation degree defined by formula (7) is introduced to judge the aggregation of individual fish [9].

$$\sigma = \frac{1}{D} \sum_{j=1}^D \left( \frac{f_j - f_{avg}}{f} \right)^2 \quad (7)$$

In the formula,  $f_j$  is the fitness function value of individual fish  $X_j(t)$ ,  $f_{avg}$  is the average fitness value of population, and  $f$  is the normalized parameter. In the early stage of identification, the individual fish in the fish swarm have great difference, including loose distribution, low clustering degree and large value.

In the later stage of optimization, the fish flock clustering degree increases and aggregation degree  $\sigma$  is higher. When  $\sigma$  is less than the threshold value, aggregation degree of the fish swarm is very high. The fusion algorithm has entered the later stage of rapid convergence of CAFS, and then it can be turned into BPNN for precision optimization.

Fig.5 is the change curve of aggregation degree  $\sigma$  in the iteration process of CAFSBPNNa, and CAFS-BPNNa-base is the original curve of iteration optimization. CAFS-BPNNa- $\sigma$  is an

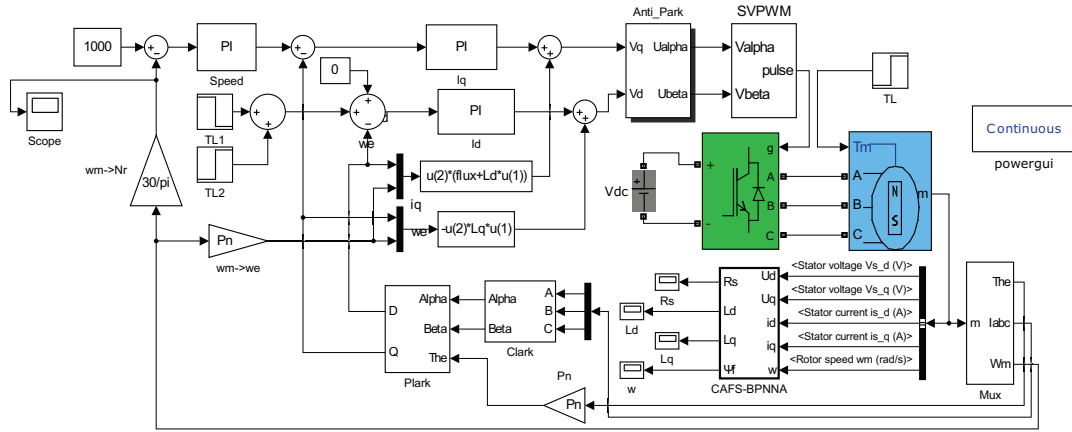


Figure 6: The block diagram of PMSM speed control system based on CAFS-BPNN

iterative curve with the judgment of population aggregation degree  $\sigma$ . After the first curve is below 0.0001, the CAFS fish swarm optimization enters the disordered state until it reaches the preset iteration number of 50 and then turns to BPNN to search for the global extremum quickly.

The latter iteration curve adds the optimum iteration of judging the degree of population aggregation  $\sigma$  to switch directly to another BPNN optimization algorithm after  $\sigma$  drops below 0.0001, and reaches the extremum point after fast convergence.

The comparison results show that the iteration optimization which combines the judgment of population aggregation degree  $\sigma$  can effectively avoid the disordered swimming in the later optimization stage of the fish swarm algorithm and improve the convergence speed of the fusion algorithm.

## 5 Result and analysis

### 5.1 Experimental setting of PMSM motor parameter identification

Table 3: Nominal parameters of PMSM motors

Parameter	Value	Parameter	Value	Parameter	Value
$P/W$	2600	$\omega/r \cdot \min^{-1}$	2000	$R_s/\Omega$	2.875
$\psi_f/Wb$	0.175	$I/A$	4	$T/N \cdot m$	5
$L_d/mH$	8.5	$J/kg \cdot m^2$	$0.48e^{-5}$	$U/V$	380
$\omega_{max}/r \cdot \min^{-1}$	2500	$L_q/mH$	8.5	$P_p/p$	4

The PMSM speed control system based on speed closed-loop control regulation is constructed on the motor control platform, as shown in Fig.6. The parameters of PMSM motor are as shown in Tab.3.

The range of parameters to be determined is  $R_s \in (0, 5), L_d \in (0, 015), L_q \in (0, 015), \psi_f \in (0, 3)$ .

The motor adopts SVPWM control strategy and the pulse current(-2A) injected into the d-axis at 0.1s lasts 5 ms. Fig.7 shows the speed tracking curve of the motor when the current pulse is injected at  $\omega = 2000r/min$ .

The data show that the speed fluctuation of the motor after the instantaneous pulse input is less than 0.5%, and the influence on the system can be neglected. Data0 and Data1 are generated

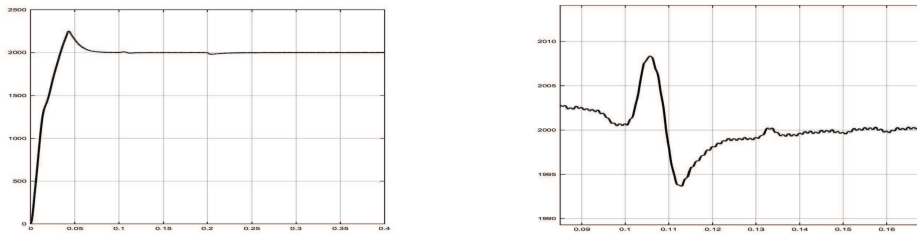


Figure 7: PMSM motor speed  $\omega$  at pulse current  $I_d=-2A$

by sampling  $\{u_d, u_q, i_d, i_q \text{ and } \omega\}$  before and after pulse current injection, and 500 groups are sampled as training and testing sets of CAFSBPNN.

## 5.2 Experimental setting of PMSM motor parameter identification

The parameters of CAFSNN algorithm are as follows: the input neuron number  $n = 9$ ; the hidden neuron number  $m = 15$ , and Tansig taken as transfer function; output neuron number  $l = 4$ , and linear purelin taken as transfer function. The training error is calculated by  $WMSE$ .

Connection weight updating is calculated by cumulative error method of adaptive inertial momentum. Intelligent fish swarm settings include: the fish swarm number  $AF\_Num = 30$ , individual fish size dimension  $D = 216$ , visual field range  $Visual = 1$ , maximum step size  $Step = 0.5$ , crowding factor  $\Delta = 14$ , maximum iteration number  $imax = 400$ , training sample 400 groups, minimum allowable training error is 0.001.

In order to compare the performance of PMSM motor parameter identification based on CAFSBPNN algorithm, RLS and PSO are introduced for analogy identification. RLS parameter configuration: learning factor  $C_1 = C_2 = 2$ , inertia weight  $W = 0.5$ , the maximum number of iterations is 400. PSO parameter configuration: estimate  $\hat{\Theta}(0) = 1 \frac{n}{P_0}$ , covariance  $P_0 = p_0 I, p_0 = 10^6$ , the maximum number of iterations is 400.

## 5.3 Training error analysis based on motor speed and torque

The speed and torque of PMSM motor are the two main indexes that affect the performance of the motor. Therefore, in the experiment, the motor is set in different conditions of speed and torque to compare the identification ability of various intelligent algorithms for motor parameters. Fig.8 is PMSM motor speed  $\omega = 2000r/m$  and load torque is  $2N \cdot m$ . The three intelligent algorithms in this paper track and compare the waveforms of motor parameter identification effect and iteration times. Tab.4 gives the identification error data of three algorithms for motor under normal speed of  $2000r/m$  and maximum speed of  $2500r/m$ , as well as Torque is  $2N \cdot m$  and  $3N \cdot m$ .

Fig.8 shows that RLS has the worst convergence performance. It usually needs 150 iterations to reach the convergence point of all identification parameters. PSO has better convergence effect, but its convergence accuracy is not high compared with other two algorithms. Compared with RLS and PSO, the proposed CAFSBPNN algorithm has better convergence time and accuracy.

When the torque value is fixed to  $2N \cdot m$  and the speed is adjusted to the maximum speed, the total training error of the three algorithms decreases, among which the RLS decreases the most, the CAFSBPNN algorithm changes the least and the identification accuracy is the highest. When the speed is fixed at  $2000r/m$  and the torque is increased by  $1N \cdot m$ , the single error of PSO arithmetic fluctuates, the errors of  $R_s$  and  $L_d$  become larger, the errors of  $L_q$  and  $\psi_f$  become smaller, and the total error increases. The  $\psi_f$  of RLS and CAFSBPNN is basically constant,

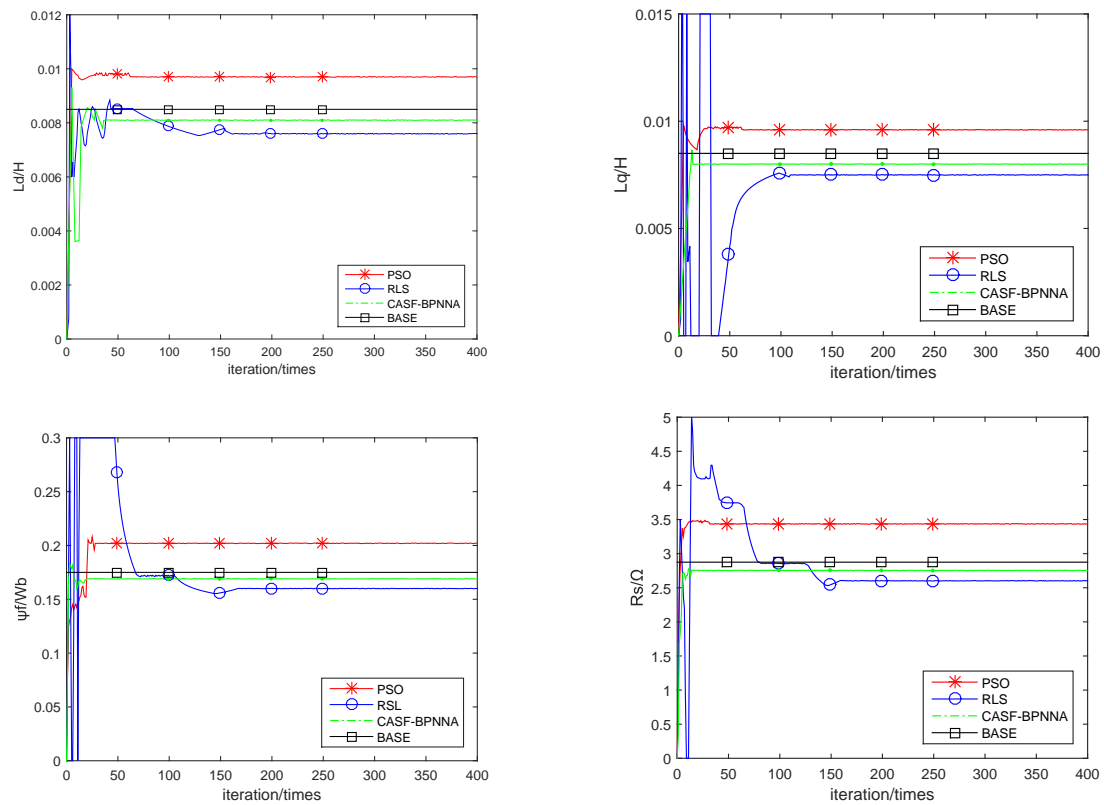


Figure 8: PMSM motor parameter identification results ( $\omega = 2000r/min, T = 2N \cdot m$ )

and the total training error decreases with the decrease of  $R_s, L_d$  and  $L_q$ . CAFSBPNN has the smallest change and the highest accuracy.

In summary, compared with RSL and PSO, CAFSBPNN is superior to the other two reference algorithms in parameter identification under uniform working conditions and error fluctuation under changing working conditions, and it always shows good convergence and identification accuracy.

Table 4: PMSM motor parameter identification error

Working condition	Algorithm	$R_s/\Omega$	$L_d/mH$	$L_q/mH$	$\psi_f/Wb$	Error
$T = 2N \cdot m$ $\omega = 2000r/min$	PSO	0.554/19.3%	1.185/13.9%	1.113/13.1%	0.009/5.2%	12.8%
	RSL	0.741/25.8%	1.343/15.8%	1.181/13.9%	0.078/44.8%	25.1%
	CAFBNNA	0.132/4.6%	0.365/4.3%	0.467/5.5%	0.007/4.5%	4.7%
$T = 2N \cdot m$ $\omega = 2500r/min$	PSO	0.477/16.6%	0.552/6.5%	1.147/13.5%	0.012/7.1%	10.9%
	RSL	0.293/10.2%	1.011/11.9%	0.629/7.4%	0.072/41.3%	17.7%
	CAFBNNA	0.129/4.5%	0.229/2.7%	0.382/4.5%	0.006/3.8%	3.8%
$T = 3N \cdot m$ $\omega = 2000r/min$	PSO	0.684/23.8%	1.198/14.1%	0.824/9.7%	0.008/4.9%	13.1%
	RSL	0.514/17.9%	1.037/12.2%	0.663/7.8%	0.081/46.8%	21.1%
	CAFBNNA	0.117/4.1%	0.365/4.3%	0.314/3.7%	0.007/4.4%	4.1%

## 6 Conclusion

Aiming at the identification of PMSM motor parameters  $R_s, L_d, L_q$  and  $\psi_f$ , the full rank identification model of motor parameters is derived based on PMSM motor voltage equation and flux equation. The feasibility of motor parameters identification by d-axis current injection in steady state and the sampling method of sample data set are analyzed. A method of parameter identification of PMSM motor by optimizing BPNN with CAFS is proposed. Compared with PSO and RLS, experiments show that the proposed CAFSBPNN algorithm has high accuracy and short convergence time for motor parameter identification, and has the stability of identification when working conditions are changed.

The specific advantages are as follows:

(1) The CAFSBPNN algorithm fully coordinates the local and global search performance advantages of BPNN and CAFS, speeds up the convergence speed and improves the convergence of motor parameter identification.

(2) The application of chaotic search reduces the sensitivity of initial value of parameter identification and enhances the robustness of parameter setting in the learning process.

(3) The CAFSBPNN algorithm has good stability, and can maintain good identification effect under different speed and torque conditions.

CAFSBPNN algorithm has good versatility. It can be used not only for parameter identification of PMSM motor, but also for parameter identification and on-line tracking of other motors such as stepping motor, induction motor and precision motor. CAFSBPNN algorithm proposed in this paper is more computational than on-chip system resources. The system adopts online sampling and periodic uploading of motor operation data. The parameters of identification network are optimized and updated by off-line optimization and remote download. Later on-chip system is implemented. In the future, the online optimization and updating methods of network parameters are further studied on the basis of improving the performance of on-chip system and optimizing the time and space complexity of algorithm.

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