A Fault-Tolerant Scheduling Algorithm using Hybrid Overloading Technology for Dynamic Grouping based Multiprocessor Systems


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Abstract:
In order to extend the application area of fault-tolerant scheduling algorithm based on hybrid overloading for multiprocessor and increase the fault-tolerant number of processors, we propose a new fault-tolerant scheduling algorithm, which is based on hybrid overloading and dynamic grouping for multiprocessor by combining logic grouping strategy for processors in primary backup overloading and backup backup overloading. This algorithm presents the formalization of the dynamic grouping for processors in fault-tolerant scheduling based on hybrid overloading and enlarges the task number included in overloading task link. In the process of fault-tolerant scheduling the processors are dynamically divided into some groups based on overloading task link, so as to keep good scheduling success ratio and enhance the fault-tolerant performance of processors. Both theoretical analysis and simulation experiment prove this algorithm’s effectiveness respectively.

Keywords: dynamic grouping; fault-tolerant; overloading; primary backup; backup backup

1 Introduction

Real-time embedded system has been applied in many fields such as military, aeronautics, astronautics and communication, and the relevant research also has made important progress. The result of task scheduling in real-time system lies on not only scheduling correctness but also time restriction. The multiprocessor platform of real-time system takes advantage of the technology of resource redundancy and time redundancy in order to meet the demand of scheduling correctness and system reliability, among them primary-backup overloading (PB) [1, 2] and backup-backup overloading (BB) [2–4] approach is most important one. Supposing that there is just a processor fault in same period, the scheduling time of different versions of different tasks is overloaded in scheduling period of same processor for PB overloading, and the scheduling time of backup-backup versions of different tasks is overloaded in scheduling period of same processor for BB overloading. The fault-tolerant scheduling technology of hybrid overloading [2, 6–8] is the combination of PB overloading and BB overloading with better scheduling efficiency and fault-tolerant performance of processor, but still supposing there is only a processor fault in same period. Logic grouping strategy [1] for processor based on PB overloading and BB overloading dynamically divides processors into groups in the process of task scheduling so as to tolerate a processor fault in every group, which is more adaptable to apply practically. But this strategy yet supposes the task number of overloading task chain is not more than two tasks, therefore the assigning of grouping size and group number is not enough flexible to be suited for hybrid...
overloading. In order to simplify the application of overloading method in scheduling algorithm, some basic application principles of overloading technology were introduced. [2]

In this paper Dynamic Grouping PB-BB Algorithm (DG_PB-BB Algorithm) combines the advantage of two overloading scheduling technology and logic grouping in the precondition of application principle for overloading technology, not only efficiently improving the efficiency of task scheduling but also enlarging tolerance area of the process. DG_PB-BB Algorithm has better application value than no grouping algorithm and logic grouping algorithm.

2 System Model

System is composed of \( m \) same processor nodes based on real time multiprocessor platform with shared memory, centralized dispatcher and processor communication medium without communication cost. Processor responsible for scheduling is dispatcher and responsible for execution is executer, which runs in parallel with dispatcher. New real time task is received by dispatcher and centralized dispatched to form assignment queue to execute on each processor.

Real time tasks to be scheduled are independent aperiodic and nonpreemptable scheduling with primary-backup copy technology. Each task \( t_i \) has two versions, namely primary copy \( pr_i \) and backup copy \( bk_i \) with identical attributes and resource requirements. Task sets \( \tau = \{ t_i | i = 1, 2, \ldots, n \} \), \( t_i = (a_i, r_i, c_i, d_i) \), \( a_i \) is the start time of task \( t_i \), \( r_i \) is the ready time of task \( t_i \), \( c_i \) is the maximal execution time of task \( t_i \), \( d_i \) is the deadline time of task \( t_i \). Processor sets \( \omega = \{ p_i | i = 1, 2, \ldots, m \} \). \( pr_i \rightarrow bk_i \) is task chain, if other tasks are overloading scheduled on task \( t_i \), then it is overloading task chain. The parameters of system model are defined as follows:

**Definition 1.** \( st(t_i) \) is the start scheduling time of task \( t_i \). \( ft(t_i) \) is the finish scheduling time of task \( t_i \). \( r_i \leq st(pr_i) \leq ft(pr_i) \leq st(bk_i) \leq ft(bk_i) \leq d_i \).

**Definition 2.** \( proc(pr_i) \) is the processor on which the primary task is scheduled, \( proc(bk_i) \) is the processor on which the backup task is scheduled, \( proc(pr_i) \neq proc(bk_i) \).

**Definition 3.** \( s(t_i) \) is the time interval on which the primary or backup task is scheduled. \( s(pr_i) \cap s(bk_i) = \phi \).

**Definition 4.** \( n_{cascade} \) is the cascade number of overloaded tasks within a processor group and a time slot. \( groupsize(g_i) \) is the processor number of a processor group \( g_i \). \( n_{cascade} = 1 \) represents the scheduling assignment of no task overloading, \( n_{cascade} = groupsize(g_i) \) represents the task can not be overloading scheduled. \( 1 \leq n_{cascade} \leq groupsize(g_i) \).

**Definition 5.** \( t_{overload} \) is the part time of a task overloaded on other tasks. \( 0 \leq t_{overload} \leq c_i \).

3 A Fault-tolerant Scheduling Algorithm Using Hybrid Overloading Technology for Dynamic Grouping Based Multiprocessor Systems(DG_PB-BB)

This paper states the strategy of dynamic grouping of fault-tolerant processor based on fault-tolerant scheduling technology of hybrid overloading and the finishing of task scheduling with the help of AP(Allocation Parameter) [5,6]algorithm. In DG_PB-BB Algorithm the system can tolerate more than two processor faults at same moment and the tasks of overloading chain can not again be limited as two numbers.
3.1 Validity checking

1. Backups can be overloaded on any task. Primaries can be overloaded only on backups.

2. If a primary $pr_i$ is overloaded on a backup $bk_j$, then $st(pr_i) \geq ft(pr_j)$.

3. A overloading task chain should not be looped. A overloading task chain is relating to some processors and the maximal primary number of a overloading task chain is $\text{groupsize}(g_i) - 1$ in the group $g_i$.

4. No more than one processor is belong to different processor groups. Every processor group has at least two processors.

5. The size of every processor group is possibly unequal and dynamically changes in the process of task scheduling.

6. The backups and primaries of same task are scheduled on same processor group. Overloading scheduling of task copy can only happen within same processor group.

7. If $\text{proc}(pr_i) = \text{proc}(pr_j)$ within same processor group, then $s(bk_i) \cap s(bk_j) = \emptyset$, stating the scheduling time of task $bk_i$ and $bk_j$ cannot be overlapping.

3.2 Scheduling algorithm

Next specifically describing DG_PB-BB algorithm. In DG_PB-BB algorithm processor grouping is concluded as four conditions, formalizably described as following:

1. If the copy of task $t_i$, $pr_i$ and $bk_i$ are not overloaded on other tasks, then the processors occupied by two copies form a new processor group $g_e$.

   $g_e = \text{form\_group}($\text{proc}(pr_i),\text{proc}(bk_i))$.

2. If $pr_i$ is not overloaded on other tasks, but $bk_i$ is, then the task chain in which task $t_k$ overloaded on $bk_i$ is situated links with the task chain in which $pr_i \rightarrow bk_i$ is situated to extend as a new processor group $g_e$.

   $(\text{proc}(pr_k),\text{proc}(bk_k)) \in \text{group}(g_e)$, $\text{expand\_group}(g_e, \text{proc}(pr_i))$.

3. If $bk_i$ is not overloaded on other tasks, but $pr_i$ is, then the task chain in which task $t_k$ overloaded on $pr_i$ is situated links with the task chain in which $pr_i \rightarrow bk_i$ is situated to extend as a new processor group $g_e$.

   $(\text{proc}(pr_k),\text{proc}(bk_k)) \in \text{group}(g_e)$, $\text{expand\_group}(g_e, \text{proc}(bk_i))$.

4. If both of $pr_i$ and $bk_i$ is overloaded on other tasks, then the task chain in which task $t_k$ overloaded on $bk_i$ is situated links with the task chain in which task $t_j$ overloaded on $pr_i$ is situated to extend as a new processor group $g_e$.

   $(\text{proc}(pr_j),\text{proc}(bk_j)) \in \text{group}(g_e)$, $(\text{proc}(pr_k),\text{proc}(bk_k)) \in \text{group}(g_f)$, $g_e = \text{expand\_group}(g_e, g_f)$.

Fig.1 states four conditions of dynamic processor grouping. OTC is overloading task chain. OTC(A) represents task chain $pr_1 \rightarrow bk_1$ and the processors occupied by it form a new processor group, which is the first condition of dynamic processor grouping. Within OTC($B_1$), the task chain $t_4$ is situated in links with $pr_3 \rightarrow bk_3$ task chain and the processors occupied by it form
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Figure 1: dynamic processor grouping

a new processor group, showing the second condition of dynamic processor grouping. Within OTC($B_2$), the task chain $t_4$ is situated in links with task chain $pr_2\rightarrow bk_2$ and the processors occupied by it form a new processor group, expressing the third condition of dynamic processor grouping. Within OTC($B_1$), task chain $pr_3\rightarrow bk_3$ links with both task chain $t_2$ and $t_4$, and the processors occupied by it form a new processor group, which is the fourth condition of dynamic processor grouping.

DG_PB-BB algorithm is based on AP scheduling strategy of hybrid overloading. New tasks form ready scheduling queue according to FCFS(First Come First Server) method. Bigger The distance of start scheduling time between primaries and backups, smaller the effect of backups to task receiving ratio, and it means start scheduling time of primaries is as early as possible, $st(pr_i)\rightarrow r_i$, finish scheduling time of backups is as late as possible, $ft(bk_i)\rightarrow d_i$. In order to increase task receiving ratio, tasks contained in task sets of hybrid overloading should be as much as possible and scheduling time occupied by them should be as few as possible. In the process of task scheduling the strategy of dynamic processor grouping is adopted to enhance tolerant level of the processor. The principle of processor grouping is the processors occupied by every overloading task chain constitute one group, if new overloading task chain has no relationship with old overloading task chain, then it should add a new processor to schedule new overloading task chain again to form a new processor group.

If $e=\text{groupsize}(g_e)$, then:

\[
AP[pr_i, p_j, ft(pr_i)] = \begin{cases} 
\frac{d_i - ft(pr_i)}{d_i - r_i} & 1 < n_{\text{cascade}} \leq e \\
\frac{d_i - ft(pr_i) - n_{\text{cascade}}t_{\text{overload}}}{d_i - r_i} & n_{\text{cascade}} = 1 
\end{cases}
\]

\[
AP[pr_i, p_j] = \max \{ AP[pr_i, p_j, ft(pr_i)] \}
\]

\[
AP[bk_i, p_j, st(bk_i)] = \begin{cases} 
\frac{st(bk_i) - r_i}{d_i - r_i} & 1 < n_{\text{cascade}} \leq e \\
\frac{st(bk_i) - r_i - n_{\text{cascade}}t_{\text{overload}}}{d_i - r_i} & n_{\text{cascade}} = 1 
\end{cases}
\]

\[
AP[bk_i, p_j] = \max \{ AP[bk_i, p_j, st(bk_i)] \}
\]

AP[$pr_i, p_j, ft(pr_i)$] is evaluation factor of scheduling scheme that a new primary $pr_i$ is assigned to schedule on processor $j$. similarly, $AP[bk_i, p_j, ft(bk_i)]$ is evaluation factor of scheduling scheme that a new backup $bk_i$ is assigned to schedule on processor $j$. AP is bigger, showing that the scheme of scheduling assignment is more optimal and scheduling efficiency is better.

DG_PB-BB Algorithm

1. The copy of first task, $pr_i$ and $bk_i$ are assigned respectively processor $p_1$ and $p_2$ to form a new group $g_e$. $g_e$ is present processor group, $G$ is assigned processor group.

 $$\text{schedule}(pr_i)\rightarrow p_1, \text{schedule}(bk_i)\rightarrow p_2, g_e=\text{form}_\text{group}(p_1, p_2), \text{validity}(), G=g_e.$$ 

2. (1) Within assigned processor group $G$, next task $t_i$ finishes scheduling with the adoption
of scheduling technology of hybrid overloading and allocation parameter.
for task $t_i$, 
while validity()$\neq$ failed
$AP(pr_i,p_{j1})=\text{next}[\text{max}(AP(pr_i,p_j))]|or AP(bk_i,p_{j2})=\text{next}[\text{max}(AP(bk_i,p_j))]$, $p_j \in \text{group}(G), j = 1,2,\cdots ,m, j_1 \neq j_2$.
schedule($pr_i$)$\rightarrow p_{j1}$, schedule($bk_i$)$\rightarrow p_{j2}$, validity().

(2) If task $t_i$ can not be scheduled within assigned processor group, then it should be to 
add a new processor into assigned processor group $G$ to schedule task $t_i$ again and 
judge whether new and old overloading task chain can be united according to four 
conditions. Otherwise to judge whether task chain $pr_i\rightarrow bk_i$ and task chain included in 
processor group $G$ are separated each other, and whether processor group $g_e$ formed 
by task chain in which task $t_i$ is situated is really contained in group $G$. If it is 
true, then group $g_e$ should be decomposed, otherwise task $t_i$ is dealt with according 
four conditions. After processors are assigned completely, if new task can not be 
scheduled, then fault-tolerant scheduling algorithm of dynamic grouping is started 
again according to principle of processor grouping.

if schedule($t_i$)$=$ failed in $G$
then {for new processor $p_k$, $G=p_k\cup G$, go to (1) (constraint $p_k = p_{j1} \lor p_k = p_{j2}$)
if (combine(link($pr_i\rightarrow bk_i$),(group($G$)$\rightarrow$ link)))$=$ failed)
then condition 1, validity()
else condition $i$, validity(), go to (1) until $j_1 \lor j_2 = m$
else
{if ((combine(link($pr_i\rightarrow bk_i$),(group($G$)$\rightarrow$ link))=$=$ failed) and
form_group($pr_i,bk_i$)$\in$ group($G$))
then decompose(form_group($pr_i,bk_i$))
else condition $i$, validity(), go to (1) until $j_1 \lor j_2 = m$
}

Next giving an example of DG_PB-BB algorithm to express the thinking of algorithm.
$T_1=(2,2,2,7.5), T_2=(4,4,2,8), T_3=(4.5,4.5,2,9), T_4=(5,5,2,10), T_5=(5.5,4.13), T_6=(6,6,3.5,14.5), m=6$. Fig.2 describes DG_PB-BB algorithm scheduling example of above queue.

![Figure 2: DG_PB-BB algorithm](image)

Firstly $m=2$, processor $p_1$ and $p_2$ form group $g_1$. $\text{St}(pr_2)=4, m=3, \text{proc}(bk_2)=p_3, pr_2$ and 
$bk_1$ can be PB overloading, $p_3$ is added into group $g_1$. $\text{St}(pr_3)=4.5$. If $m=3, pr_3$ and $bk_3$ can not 
be scheduled within group $g_1$, then $m=4, bk_3$ and $bk_2$ are BB overloading, $\text{proc}(pr_3)=p_4, p_4$ is 
added into group $g_1$. $\text{St}(pr_4)=5, m=4, pr_4$ and $bk_4$ can be scheduled within group $g_1, \text{proc}(pr_4)=p_1$. 

proc(bk₄)=p₂, and task chain pr₄→bk₄ is separated from old overloading task chain within group g₁ and really included in group g₁, so that task chain pr₄→bk₄ is combined into group g₁. st(pr₅)=5, m=4, pr₅ and bk₃ can not be scheduled within group g₁, so it is to extend a new processor p₅ and rescheduling pr₅ and bk₅ within processor scheduling sets composed of p₅ and group g₁. proc(pr₅)=p₅, proc(bk₅)=p₄. As a result, task chain pr₅→bk₅ is separated from old overloading task chain within group g₁ and not really included in group g₁, therefore it is to extend task chain pr₅→bk₅ as group g₂. st(pr₆)=6, task t₄ can not be scheduled neither in group g₁ nor group g₂, so that a new processor p₆ is added into group g₂ and task t₄ is rescheduled within extended group g₂, proc(pr₆)=p₆, proc(bk₆)=p₄, bk₅ and bk₆ is BB overloaded on processor p₄. All processors have been assigned completely so that DG_PB-BB algorithm is restarted from processor p₁ while there are new tasks arriving into scheduling queue.

3.3 Algorithm analysis

If task sets showed in Fig.2 are scheduled by AP scheduling algorithm of hybrid overloading without grouping(PB-BB_AP Algorithm), although it only needs four processors to finish scheduling, but can just tolerate a processor fault and is too strict to apply widely. DG_PB-BB algorithm needs to increase two processors to finish scheduling, but new processor group g₂ in system makes fault-tolerant number of processor extend as two processors so as to strengthen the reliability of system. Time complexity of PB-BB_AP algorithm is $O(N^2 \cdot m \cdot (m - 1))$, N is average task number of task sets on which a processor has ever scheduled, m is processor number of the system. If in DG_PB-BB algorithm average processor number of group $g_k$ is $k$, then time complexity of DG_PB-BB algorithm is $O(N^2 \cdot k \cdot (k - 1))$. In regard to DG_PB-BB algorithm, comparing with PB-BB_AP algorithm, the algorithm cost decreases and the system reliability increases, but the guarantee ratio decreases, because PB-BB_AP algorithm is an ideal method.

3.4 Theory testification

The theory testification follows the methodology used in [8] and is based on the following assumptions:

- All tasks have unit worst execution time, for example: $c_i=1$.
- Backup slots are preallocated in the schedule.
- FIFO scheduling strategy is used.
- Task deadlines follow uniform distribution $[W_{min}, W_{max}]$, called deadline window. If $P_{win}(w)$ is the probability that an arriving task has a relative deadline $w$, then $P_{win}(w) = 1/(W_{max} - W_{min} + 1)$, $W_{min} \leq w \leq W_{max}$.
- Task arrivals follow uniform distribution $[0, A_{max}]$, with mean $A_{av}=A_{max}/2$. If $P_{ar}(k)$ is the probability of $k$ tasks arriving at a given time, then $P_{ar}(k) = 1/(A_{max} + 1)$, $0 \leq k \leq A_{max}$.

A simple pre-allocation policy for BB overloading is to reserve a slot for backups every $n$ time slots on each processor. Backup slots on the three processors can be staggered. For a task $t₄$, bk₄ is scheduled immediately after pr₄ with probability 0.5 and is scheduled two slots later than pr₄ with probability 0.5.

In PB overloading there are three different types of time(0, 1 and 2), if $(t-1)\mod 3 = i$, any time $t$ has a type of $i$. At any time $t$, the number of primaries that can be scheduled to start at that time is $s_0$ if $t$ is of type 0, $s_1$ if $t$ is of type 1, $s_2$ if $t$ is of type 2.
Using FIFO scheduling is equal to maintaining a task queue, to which arriving tasks are appended. Given that the number of task that can be scheduled on each time unit is known, then the position of a task in the Q indicates its scheduled start time. In BB overloading two tasks can be scheduled on each time (one slot is reserved for backups). If at the beginning of time slot $t$, a task $t_i$ is the $q$th task in $Q$, then $t_i$ is scheduled to execute at time slot $t+g_{q-BB}^{BB}$. $g_{q-BB}^{BB}$ is the time at which a task, whose position in the $Q$ is $q (q=1,2,\cdots,2W_{\max})$, will be executed and is defined as $g_{q}^{BB} = \left\lfloor \frac{q}{2} \right\rfloor$. In PB overloading, $s_0,s_1$ and $s_2$ tasks can be scheduled on a given time slot $t$ depending on whether $t$ is of type 0,1, or 2 respectively. The time $g_{q}^{PB}$ is defined as $g_{q}^{PB} = (i+j+1) \sum_{c=1}^{i} s_0 + \sum_{c=1}^{j} s_1 + \sum_{c=1}^{l} s_2 \leq q - 1, |i - j| \leq 1, |j - l| \leq 1, |l - i| \leq 1$. When $i \geq j \geq l$ if $t$ is of type 0, $j \geq l \geq i$ if $t$ is of type 1, and $l \geq i \geq j$ if $t$ is of type 2. When a task $t_i$ arrives at time $t$, its schedulability depends on the length of $Q$ and on the relative deadline $w_1$ of the task. In BB overloading, if $t_i$ is appended at position $q$ of $Q$ and $w_1 \geq g_q^{BB}$, then the primary task $p_{r_1}$ is guaranteed to execute before $t+w_i$. Moreover, if $w_1 \geq g_q^{BB} + 2$, then $bk_i$ is also guaranteed to execute before $t+w_i$. In PB overloading, if $t_i$ is appended at position $q$ of $Q$ and $w_1 \geq g_q^{PB}$, then the primary task $p_{r_1}$ is guaranteed to execute before $t+w_i$. Moreover, if $w_1 \geq g_q^{PB} + 2$, then $bk_i$ is also guaranteed to execute before $t+w_i$. Let $p_{q,k}$ be the probability that one of the $k$ tasks is rejected when the queue size is $q$, and its value is the probability that the relative deadline of the task is smaller than $g_{q}^{*}$. In PB overloading, $g_{q}^{PB}$ is the time at which a task, whose position in the $Q$ is $b$, will be executed in the PB-BB overloading scheduling strategy of logic grouping, $b = q + k/2$. Showing as $t_0-t_{12}$ in Fig.3, processor $p_1-p_{12}$ are divided into 4 groups and every group has 3 processors, adopting with scheduling strategy of BB overloading, processor $p_{13}-p_{24}$ are also divided into 4 group and every group has 3 processors, adopting with scheduling strategy of PB overloading. Above method is described as PB-BB overloading scheduling strategy of logic grouping.

$$
g_{q}^{logi}c = (i+j+1) \sum_{c=1}^{i} s_0 + \sum_{c=1}^{j} s_1 + \sum_{c=1}^{l} s_2 \leq q - 1, |i - j| \leq 1, |j - l| \leq 1, |l - i| \leq 1.
$$

$g_{q}^{dynamic}$ is the time at which a task, whose position in the $Q$ is $b$, will be executed in the PB-BB overloading scheduling strategy of dynamic grouping, $b = q + k/2$. Different with logic grouping, in dynamic grouping $s_0=3$, $s_1=4$ and $s_2=2$. Describe as $t_{12}-t_{24}$ in Fig.3, processor $p_1$-$p_{12}$ is divided into 3 groups and every group has 4 processors, adopting with scheduling strategy of BB overloading, processor $p_{13}-p_{24}$ are also divided 3 groups and every group has 4 processors, adopting with scheduling strategy of PB overloading. Above method is described as PB-BB overloading scheduling strategy of dynamic grouping.

$$
g_{q}^{dynamic} = (i+j+l)(n-n/3)+\sum_{c=1}^{i} s_0 + \sum_{c=1}^{j} s_1 + \sum_{c=1}^{l} s_2 \leq q + k/2 - 1, |i - j| \leq 1, |j - l| \leq 1, |l - i| \leq 1.
$$

Obviously, $g_{q}^{dynamic} < g_{q}^{logi}c$. $g_{q}^{dynamic}$ decreases more quickly than $g_{q}^{logi}c$ with increasing $n$, therefore DG_PB-BB algorithm is more efficient than LG_PB-BB algorithm with increasing $n$. 


4 Simulation Experiment

Supposing LG_PB-BB represents fault-tolerant scheduling algorithm of hybrid overloading based on the strategy of logic grouping. Simulation experiment mainly compares with change situation of the guarantee ratio ($GR$) in variety of fault-tolerant number of processor in circumstance of different task load for DG_PB-BB, LG_PB-BB and PB-BB_AP algorithm respectively. The guarantee ratio—the number of tasks guaranteed/the number of tasks arrived. Simulation parameters as following:

- The inter-arrival time of tasks follows exponential distribution with mean $\theta$. $\theta = 8$.
- The inter-arrival time of faults follows exponential distribution with mean $\lambda$. $\lambda = 200$.
- The execution time of a task is chosen uniformly $[2,8]$.
- The deadline of a task is chosen uniformly $[r_i + c_i, r_i + R * c_i]$, where $R \geq 1$.
- Processor number $m = 10$, task number $n = 50$.
- $R$(task laxity) represents flexibility time task $t_i$ can stay in ready queue in precondition of finishing scheduling before deadline. $R = 3$.
- $L$(task load) is the expected number of task arrivals per mean service time. $L = C/\theta$, $C$ is the mean execution time, $\theta$ is the inter-arrival average time of tasks $t_i$. Bigger $L$ is, more the average load of processor is and lower the guarantee ratio is.

In Fig.4 (a),(b) and (c) respectively show the relationship of processor fault and guarantee ratio in DG_PB-BB, LG_PB-BB and PB-BB_AP algorithm for the system of $L = 0.25, L = 0.5$ and $L = 1$. Experiment results prove $GR$ decreases along with $L$ and processor faults increase. When there is only one processor fault in DG_PB-BB, LG_PB-BB and PB-BB_AP algorithm, the differences of $GR$ for the system of $L = 0.25, L = 0.5$ and $L = 1$ are small. When processor fault increases to more than two faults, $GR$ for three kinds of task load in PB-BB_AP algorithm are all low and failure possibility of task scheduling is high. When $L = 0.25$ and $L = 0.5$ in DG_PB-BB algorithm $GR$ enhances significantly comparing with LG_PB-BB algorithm, and for the system of $L = 1$ the difference of $GR$ between two algorithm is small, stating in the system of not full load task DG_PB-BB algorithm can tolerate processor fault better than LG_PB-BB and PB-BB_AP algorithm.
5 Conclusions

This paper improves task number and grouping strategy included in overloading task chain and proposes DG_PB-BB algorithm based on PB-BB_AP algorithm according to logic grouping strategy of PB overloading and BB overloading. Simulation experiment shows DG_PB-BB algorithm not only has good guarantee ratio of task scheduling, but also improves fault-tolerant level of processor, with better application valuation.
Main creative achievements include 1) introducing the formalization of processor dynamic grouping in fault-tolerant scheduling technology of hybrid overloading, 2) proposing the method of processor dynamic grouping based on overloading task chain, and 3) extending task number included in overloading task chain and increasing fault-tolerant level of processor by the adoption of processor dynamic grouping.

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